

## Midterm Exam II

Fall 2013, MAT172 Section B401[19441]

November 5th, 2013. 9:00AM–10:40AM.

**Instructions:** Print your name on the exam booklet. This exam is closed-book and closed-note. You cannot use any electronic device in this exam. You are not allowed to talk to other students. Write all details explicitly. Answers without justifications and/or calculation steps may receive no score. Hand-in blue booklet only, and keep the exam paper for your study.

- 1.(Sample Final I-5) Draw the graph of  $y = 3x^2 + 6x + 10$  and label its minimum.(4 points)
- 2.(Sample Final I-5) Draw the graph of  $y = -2x^2 + 8x + 2$  and label its maximum.(4 points)
- 3.(Sample Final I-9) Write an equation of the parabola given its graph in Figure 1.(4 points)
- 4.(Sample Final I-9) Write an equation of the parabola given its graph in Figure 2.(4 points)
- 5.(Sample Final I-10) Let  $f(x) = 2e^{x-1}$ . Write the inverse of  $f$  and specify its domain.(4 points)
- 6.(Sample Final I-10) Let  $g(x) = \frac{1}{2}e^{3x}$ . Write the inverse of  $g$  and specify its domain. (4 points)
- 7.(Sample Final I-16) If a publisher charges \$50 for a textbook, she will sell 8000 copies. For each \$1 she raises the price, she sells 100 fewer copies, and for each \$1 she lowers the price, she sells 100 more copies.
  - (1) How much should she charge to maximize revenue?(6 points)
  - (2) How many books will she sell at that rate?(2 points)
- 8.(Sample Final I-16) Sixty meters of fencing are to be used to enclose a rectangular garden. Find the dimensions that will give the maximum area.(8 points)
- 9.(Sample Final I-16) The revenue from the sale of  $x$  items is  $R(x) = 800x - 2x^2$  dollars and the cost to produce these  $x$  items is  $C(x) = 2x^2 + 1000$  dollars. How many items should be produced to maximize profit?(8 points)
- 10.(Sample Final I-17) There are 100 bacteria in a culture, and the number of bacteria triples every 5 hours.
  - (1) How many will there be in 30 hours?(2 points)
  - (2) Write a function that gives the number of bacteria  $t$  hours from now.(3 points)
  - (3) In how many hours will there be 1800 bacteria?(3 points)

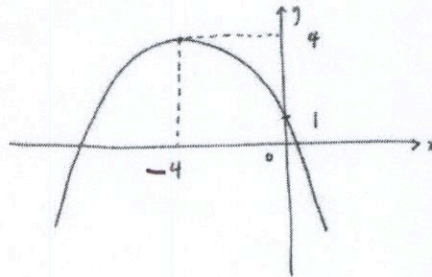


Figure 1: Problem 3

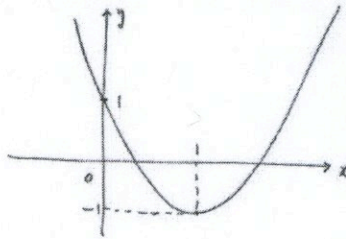


Figure 2: Problem 4

11.(Sample Final I-17) The population of West Oblivion was 600 in 1850 and is known to double every 25 years.

- (1) What was the population in 2000?(2 points)
- (2) Write a function,  $P$ , that gives the population  $y$  years after 1850.(3 points)
- (3) In what year did the population first exceed 4000?(3 points)

12.(Sample Final I-17) A bank account receives 3% annual interest compounded quarterly. If \$1000 is deposited into the account initially and no other deposits are made, write a formula for  $D$ , the amount of money in the account after  $t$  years. How many years will it take for the amount of money in the account to double?(8 points)